

Mathematics of Finance

Why is interest paid??

- Opportunity cost
- Inflation
- Liquidity preference
- Risk factor
- Time value of Money

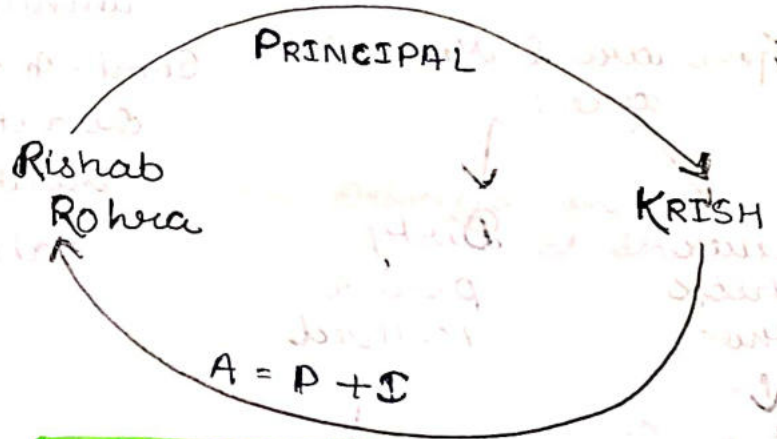
Lend Money → Return

Interest →

Extra Money Receive

Definitions

- Interest
- Principal
- Accumulated amount (Balance)
- Rate of Interest
- Time period



$$\% = \frac{I}{P} \times 100$$

SIMPLE INTEREST

$$S.I = \frac{P \times R \times T}{100}$$

NOTE → Simple interest is calculated on principal for every time period whereas, C.I is calculated on accumulated amount of previous time period.

Compound Interest

$$A = P \left(1 + \frac{r}{100}\right)^t$$

as per C.I

when compounding annually.

$$A = P + C.I$$

$$C.I = A - P$$

$$C.I = P \left(1 + \frac{r}{100}\right)^t - P$$

$$P \left[1 + \frac{r}{100}\right]^t - 1$$

calculator Trick

Limitation: when $t \leq 5$ years

$$A = P + \underbrace{r\% + r\% + r\%}_{\geq 5}$$

conversion period

compounding $\frac{1}{c}$ (no. of conversion in year)

Annually :- 1

Semi-Annually :- 2

Quarterly :- 4

Monthly :- 12

Daily :- 365

If question mentioned of C.I not about time period and if assume compound will be annually.

There are 2 Method are:

Power check Method

Dirty power Method

$$(x)^n = (y)^m$$

$$y^x = \dots x$$

Power check Method use only when option have no decimal Method.

If option have decimal number.

$a^{\frac{1}{n}} \rightarrow$ Type 'a'

$\rightarrow \sqrt{\quad}$ 12 times

$\rightarrow - 1$

$\rightarrow \div n$

$\rightarrow + 1$

$\rightarrow 'x ='$ 12 times

LOGARITHM Method

$(a)^{\frac{1}{n}} \rightarrow \log a$
 \downarrow
 $\sqrt{\quad}$ 15 times
 \downarrow
 \log

$$\boxed{\times 14230}$$

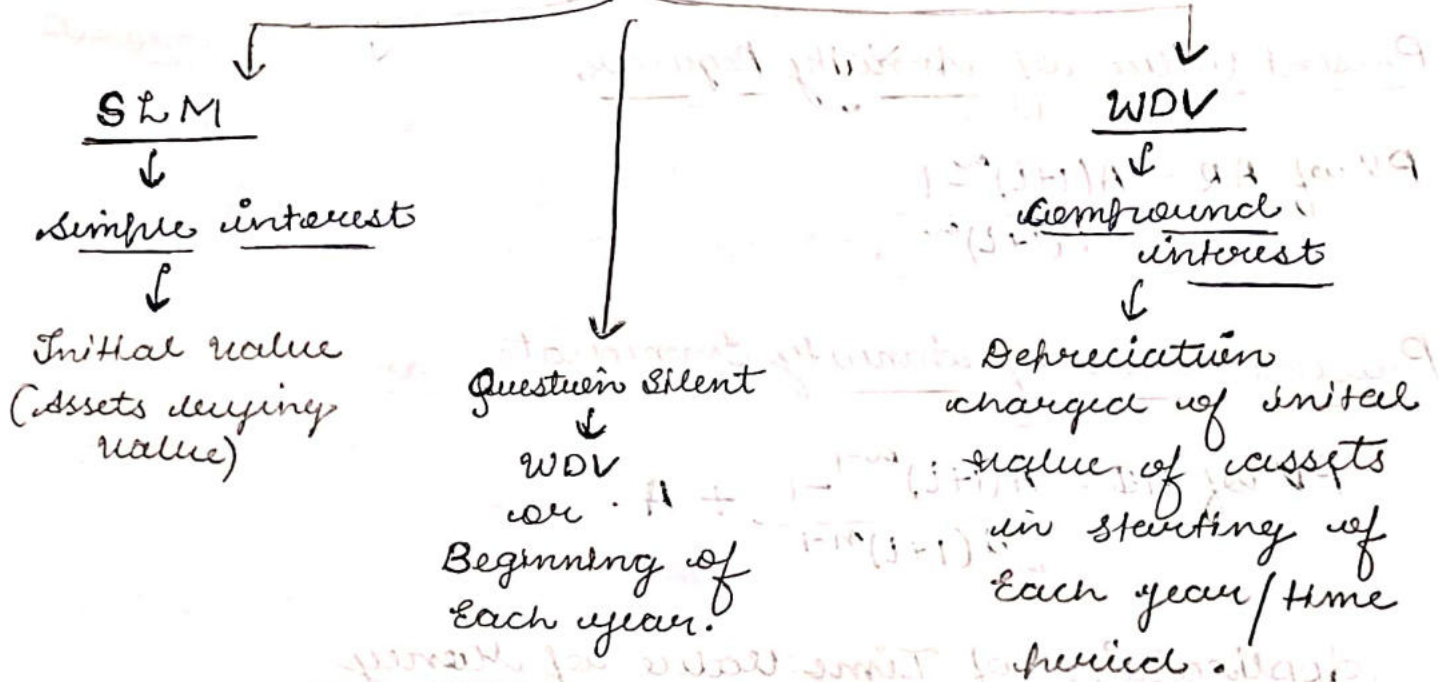
Effective Rate of Return

$$\text{Rate of Interest} = \frac{\text{Interest}}{\text{Principle}} \times 100$$

$$E.R.I = \frac{P[(1+i)^n - 1]}{P} \times 100$$

$$E.R.I = [(1+i)^n - 1] \times 100$$

Depreciation



Annuity

Annuity regular/
Annuity certain

↓
1st annuity paid will be in end of first period.

Annuity due/
Annuity immediate

↓
when first annuity paid is at the start of first period.

Future Value of Annuity Regular

$$FV \text{ of AR} = \frac{A(1+i)^n - 1}{i}$$

Future Value of Annuity Immediate

$$FV \text{ of AI} = \frac{A(1+i)^n - 1}{i} \times (1+i)$$

Present Value of Annuity Regular

$$PV \text{ of AR} = \frac{A(1+i)^n - 1}{i(1+i)^n}$$

Present Value of Annuity Immediate

$$PV \text{ of AI} = \frac{A(1+i)^{n-1} - 1}{i(1+i)^{n-1}} + A$$

Applications of Time Value of Money

- ① Sinking fund → FV of AR
- ② Leasing → PV
- ③ Capital Expenditure → PV
- ④ Valuation of Bond → PV of an + PV of single Amount
- ⑤ Perpetuity → PV of infinite payment
- ⑥ CAGR → compound interest
- ⑦ NPV → PV

Leasing

- Owner → lessor ✓
- Borrower → lessee ✓
- Time period → lease period ✓
- Annuity → lease Rental ✓

In Leasing question agar job purchase value sech upar rent value ayga toh rent preferable hogi!!!

Perpetuity

↳ Zindagi ke Sath hi Zindagi ke baad bhi.....

$$PVA_{\infty} = \frac{A}{i} \quad \left[\begin{array}{l} \text{FOREVER} \\ \text{PERPETUITY} \end{array} \right]$$

Growing Perpetuity

$$PVA_{\infty} = \frac{A}{i-g} \quad [i < g]$$

SOME DEFINITION

- Nominal rate of Return → [offered rate]
- Real rate of return
↳ [Inflation] + [Real Rate] ⇒ Int. Rate - Inflation
we offered job samne sech mila!!
- Effective rate of return → Effectiveness because of compounding.
- Discounted rate of return → used for calculating present value of future cash flow.
↓
job sumera kaise kahi future calculating ke liye karte hai ⇒ Compounding Rate

Net present value

$$PV = \frac{An}{(1+i)^n}$$

$$= An \times \frac{1}{(1+i)^n}$$

PVIF
Present value of interest factor.

$$PV \text{ of AR} = \frac{A(1+i)^n - 1}{i(1+i)^n}$$

PVFA (Present value factor accumulated)

t	year	PV = $\frac{1}{(1+i)^n}$
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$$NPV = PV \text{ of cash inflow} (-) - PV \text{ of cash outflow}$$

Net present value \rightarrow ~~the~~ PV of C.I. \rightarrow PV of C.O

$NPV \geq 0 \rightarrow$ preferable \rightarrow Accept the investment

$NPV < 0 \rightarrow$ Not preferable \rightarrow Reject the investment

Valuation of Bond

Bond issue \rightarrow Maturity period
 \rightarrow Nominal rate

V.O.B \Rightarrow PV of annuity + PV of an amount

$$= \frac{A(1+i)^n - 1}{i(1+i)^n} + \frac{An}{(1+i)^n}$$

Accumulated Amount

CAGR \rightarrow Compound Annual Growth Rate

$$A = P(1+i)^t$$

$$V_n = V_0 \left(1 + \frac{CAGR}{100} \right)^{t_n - t_0}$$

$$CAGR = \left(\frac{V_n}{V_0} \right)^{\frac{1}{t_n - t_0}} - 1 \times 100$$